Theory of Synthesis of Asymmetrical Delay Line with the Surface Acoustic Wave

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The aim of this publication is to design a procedure for the synthesis of an IDT (interdigital transducer) with diluted electrodes. The paper deals with the surface acoustic waves (SAW) and the theory of synthesis of the asymmetrical delay line with the interdigital transducer with diluted electrodes. The authors developed a theory, design, and implementation of the proposed design. They also measured signals. The authors analysed acoustoelectronic components with SAW: PLF 13, PLR 40, delay line with PAV 44 PLO. The presented applications have a potential practical use.

Keywords: delay line; diluted electrodes; surface acoustic wave; interdigital transducers; resonators.

1. Introduction

Among the perspective acoustoelectronic components with the surface acoustic waves (SAW) there are the bandpass filters, delay lines (DL), and resonators, which are used as selective elements of oscillators with harmonic oscillations (NEVESELY, 1986; HARTMANN, 1985; RUPPEL, FJELDY, 2000). The main advantage is their small size and low weight, high mechanical strength, low sensitivity to vibration as well as the possibility to make the oscillators without the use of inductor. This is what guarantees their manufacturing perspective and wide range of use in measuring of electric and non-electric variables, in radio electronics, telecommunications, and introduces the necessity of elaboration of questions concerning their theory and manufacturing.

According to the literature, delay lines can be realised by electrical or acoustic means (HASANOV, HASANOV, 2017; KIM et al., 2017; ZHU, RAIS-ZADEH, 2019).
2017; Alshaykh et al., 2017; Audier et al., 2017; Marzo et al., 2017; Young et al., 2017; Cheng et al., 2017; Gruber et al., 2016; Djoumi et al., 2016; Zhang, Hu, 2015; Tung et al., 2015; Zheng et al., 2015). The SAW delay line is used instead of transmission systems composed of a few thousands of transistors.

In the present paper the authors develop a theory of an asymmetrical delay line with interdigital transducer (IDT) with diluted electrodes.

2. Synthesis of asymmetrical delay line

An asymmetrical delay line has an input IDT with a small number of electrodes (i.e. broadband), and an output IDT with a large number of electrodes (i.e. narrowband). Module characteristic can be close to the synchronous frequency sufficiently accurately approximated by the function of

$$\frac{\sin x}{x}, \text{ where } x = N\pi\left(f - f_0\right) / f_0.$$ 

When increasing the number of electrodes IDT, however, there is a signal caused by reflections from the edges of the electrodes, which substantially impairs the delay line properties and at the same time of the whole oscillator. To suppress the signal the authors partly remove the electrodes in the narrowband IDT (i.e. “diluted” – divided into groups IDT). A similar problem arises in the synthesis of the filter with

a narrow and very narrow pass band $\Delta f_3/f_0 = 0.1$ to $0.5\%$ (n. On the contrary, the methods of synthesis of filters with SAW are accurate at a relatively wide pass band $f_3/f_0 = 1$ to $30\%$).

2.1. Frequency and time characteristics of the individual groups of electrodes in the IDT with diluted electrodes

The diluted IDT refers only to the periodic removal of the same groups of electrodes of IDT (Fig. 1a). If there is a change of the period or distance of groups and also the number, overlap, step, width, or other parameter of electrodes of the retained groups according to a certain rule which differs from the one accepted in the original IDT, then we are talking about so called weighing of electrodes and it needs to be examined separately.

In the general case, if we do not consider the discretisation in the process of sampling time, the impulse characteristic of diluted IDT can be expressed in the form of the sum of the impulse characteristics $h_m(t - t_m)$ shifted for a period of $T_r$ (Fig. 1b), i.e.

$$h_r(t) = \sum_{m=1}^{M} h_m(t - t_m),$$

where $h_m(t - t_m)$ is a function which describes the pulse characteristic of a group consisting of $N_i$ pairs of unsplit electrodes with the length $T_i$, $m$ is a group number, $M$ is the number of groups, and $t_m = mT_r$.

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**Fig. 1.** IDT with periodically diluted electrodes.
A parameter \( r = T_r / T_i \) is called substituting dilution, by analogy with the impulse modulation of signals.

In the special case of division into groups of an apodised IDT where \( a(t) \) is the apodisation function its impulse characteristics has the shape

\[
h_r(t) = \sum_{m=1}^{M} a(t) h_{mr}(t - t_m), \tag{2}
\]

where

\[
h_{mr} = \begin{cases} 
1 & \text{for } (m-1)T_r \leq t \leq (m-1)T_r + T_i, \\
0 & \text{for } (m-1)T_r + T_i \leq t \leq mT_r,
\end{cases}
\]

is a periodic sequence of the impulse characteristics of groups with the same aperture.

According to linear properties of Fourier transformation, the transfer function of the IDT with diluted electrodes represents a convolution of the transfer function \( H_{mr}(j\omega) \) of the undiluted IDT and of the spectrum of modulation function \( H_m(j\omega) \) of group and is equal to the sum of the spectra of the individual groups that are repeated with the repetition rate \( f_r = 1/T_r \).

It uses the following Eq. (3):

\[
H_r(j\omega) = \sum_{m=1}^{M} A_m(\omega) e^{j\Theta_m(\omega)} = H_{mr}(j\omega) + H_a(j\omega), \tag{3}
\]

where \( A_m(\omega) \) is module characteristics of the \( m \)-th group, \( \Theta_m(\omega) = \Theta_{mr}(\omega) + \Theta_m(\omega) \) is argument characteristics of the \( m \)-th group, \( \Theta_{mr}(\omega) \) is the initial phase of the group which is determined by the control period \( T_r \), \( \Theta_{mn}(\omega) \) is the phase change within the group.

In the periodic dilution, due to removing of electrodes within the length of the whole transducer, the phase shift of each group in the synchronous frequency is \( \omega_0 \) times \( \pi \) and the initial phase of the \( m \)-th group, \( \Theta_{mn}(\omega_0) = \omega_0T_m = \omega_0(m-1)T_r = \pi(m-1)N_rN_i \), where \( T_m = (m-1)T_0N_rT_r \) is the time coordinate of the edge of the \( m \)-th group with the respect to the edge of the transducer, \( N_r = N_i / r \) is the number of electrode pairs attributable to the spatial period \( L_r \) (Fig. 1a), \( T_{bi} = 1/(2f_0) \) is the period of location of the unsplit electrodes of the \( i \)-th group.

Let us examine the characteristics of one of non-apodised group with equidistant distribution of electrodes. If we do not consider discretisation of impulse characteristics in the process of sampling time, the equation for the transfer function \( H_{mr}(j\omega) \) group is analogous to the equation for the spectral density of videoimpulse \( T_i \). When reading from the edge of the group \( (0 \leq t \leq T_i) \), the equation in a wide frequency range of \( 0 \leq \Omega \leq \Omega_N \) has the shape

\[
H_{mr}(j\omega) = \frac{1}{j\Omega} \left(1 - e^{-j\Omega T_i}\right) + \frac{2}{\Omega} \sin \left(\frac{\Omega T_i}{2}\right) e^{-j\Omega T_i/2}, \tag{4}
\]

where \( \Omega = \omega - \omega_0 \), \( \Omega_N = \omega_N - \omega_0 \), \( \omega_N \) is the Nyquist frequency.

From this equation the module characteristics can be expressed by the relation

\[
A_m(\Omega) = \left| \frac{2}{\Omega} \sin \left(\frac{\Omega T_i}{2}\right) \right| \tag{5}
\]

and the argument characteristics which is determined by the mutual spacing of electrodes, by the relation

\[
\Theta_{mn}(\Omega) = \frac{\Omega T_i}{2} + (k - 1) \pi \tag{6}
\]

for

\[
(k - 1) \frac{2\pi}{T_i} \leq \Omega \leq (k + 1) \frac{2\pi}{T_i},
\]

where

\[
k = 1, 2, 3, ..., \frac{\Omega_N}{T_i}.
\]

In cases where readings are performed from the centre of a non apodised group \((-T_i/2 \leq t \leq T_i/2\) ), the transfer function of the group is given by the relation

\[
H_{mr}(j\omega) = \frac{1}{j\Omega} \left(e^{j\Omega T_i/2} - e^{-j\Omega T_i/2}\right) = \frac{2}{\Omega} \sin \left(\frac{\Omega T_i}{2}\right), \tag{7}
\]

from which

\[
A_m(\Omega) = \left| \frac{2}{\Omega} \sin \left(\frac{\Omega T_i}{2}\right) \right| \tag{8}
\]

and

\[
\Theta_{mn}(\Omega) = (k - 1) \pi \tag{9}
\]

for

\[
(k - 1) \frac{2\pi}{T_i} \leq \Omega \leq (k + 1) \frac{2\pi}{T_i},
\]

where

\[
k = 1, 2, 3, ..., \frac{\Omega_N}{T_i}.
\]

It results from the above that the module characteristics of the non apodised group is of the same shape, independently from the beginning of reading and the argument characteristics is linear, angled at \( 0 \leq t \leq T_i \) and stepped at \(-T_i/2 < t < T_i/2\) . If we use the model of functions \( \delta \), the impulse characteristics of the IDT, considering the discretisation, can be expressed by a sequence of functions \( \delta \) located in the centre of electrodes. Therefore, the transfer function of the apodised equidistant group, which is symmetrical relative to the centre of readings, according to the properties of the IDT with the linear phase and considering Eq. (9) is expressed by the following Eq. (10):

\[
H_{mr}(j\omega) = \left[1 + 2 \sum_{n=1}^{N} (-1)^n \gamma_{ni} \cos(\omega_n T_0 n)\right] e^{-j(k-1)\pi} \tag{10}
\]
for an odd number of electrodes in the group $A_i = 2N_i + 1$ and

$$H_{mr}(j\omega) = \left\{ j2 \sum_{n=1}^{N} (-1)^{n} \nu_{ni} \sin[\omega(n - 0.5)T_0] \right\} e^{-j[(k-1)\pi + (\omega_0 - \omega)T_e]/2}$$

(11)

for an even number of electrodes in the group $A_i = 2N_i$.

In Eqs (10) and (11), $k = 1, 2, 3, ..., N_i/T_1$, $\gamma_{ni}$ and $\nu_{ni}$ are coefficients of impulse characteristics of a group, $T_0$ is an interval of discretisation of the group. For a non apodised group $\gamma_{ni} = \nu_{ni} = 1, 0$. At a changing overlap of the electrodes, $\gamma_{ni}$ and $\nu_{ni}$ vary according to the given rule.

In the previous analysis, the authors did not consider the interaction of electrodes of the IDT and the frequency dependence of the intensity of radiation of pair of electrodes forming an elementary group.

### 2.2. Transmission properties of the diluted IDT over a wide frequency range

For the non apodised equidistant IDT, which consists of $M$ the same groups symmetrical relative to the centre, $\Theta_{mr}(\omega) = 2\pi$ and Eq. (3) can be simplified to the form

$$H_{mr} = A_m(\Omega) \sin \left( \frac{\pi \omega}{2\omega_0} \right) \left[ 1 + e^{-j\Omega T_e} + e^{-j2\Omega T_e} + ... + e^{-j(M-1)\Omega T_e} \right]$$

$$= A_m(\Omega) \sin \left( \frac{\pi \omega}{2\omega_0} \right) \sum_{m=1}^{M} e^{-j(m-1)\Omega T_e}.$$  

(12)

At frequencies satisfying the condition $\Omega_k = k2\pi/T_r = k2\pi f_r$, each addend in square brackets equals one, and if we do not consider the frequency dependence of the radiation of electrodes, the transfer function will have the shape

$$H_r \left( \frac{k2\pi}{T_r} \right) = MA_m \left( \frac{k2\pi}{T_r} \right).$$  

(13)

At frequencies $\Omega_k = k2\pi/T_r = k2\pi f_r$ (or $f_k = f_0 \pm k/T_r = f_0 \pm k f_r$) the transfer function of the diluted IDT contains partial pass bands.

Thus, the module characteristics of the diluted IDT (Fig. 1c) has, in addition to a basic pass band at frequency $f_0$, partial pass-bands at frequencies $\pm f_k$, with “the step” $f_r$, which is inversely proportional to the spatial period $L_r$. The size of partial module characteristics $A_k(f)$ varies depending on the module characteristics of the group $A_m(f)$.

### 2.3. Use of the diluted interdigital transducers

The diluted IDT can be used for the construction of narrowband filters with comblike frequency response.

In that case it is advantageous to use narrowband IDT$_1$ with diluted electrodes and broadband IDT$_2$. According to Eq. (3), the transfer function of the filter will have the range of narrowband partial passbands caused by dilution of electrodes of the IDT$_1$.

However, we require more often filters with one permeable band. Figure 2a shows schematically a narrowband filter consisting of the diluted IDT$_1$ and the broadband IDT$_2$. There are two possible variants of their arrangement. In the first one, the spatial periods $L_1$ and $L_2$ are the same, in the second one they are different ($L_1 < L_2$, $L_1 > L_2$, respectively). In a simple case it can be any group of the IDT$_1$ consisting of one pair of electrodes.

In the first case ($L = L_1 = L_2$), it must be for the suppression of partial passbands that the length of the IDT$_2$ is equal to the period of control of the IDT$_1 - L_r$. If the condition is satisfied, the zeros of the module characteristics of the broadband IDT$_2$ (Fig. 2b) are identical with maximum values of partial passbands (except for the passband at $f_0$).
the ratio of the product of $L_1$ and $L_2$ and the difference between these periods (Fig. 3a), i.e.

$$L_r = \frac{kL_1L_2}{L_1 - L_2}, \quad \text{if } L_1 > L_2,$$

(14)

and

$$L_r = \frac{kL_1L_2}{L_2 - L_1}, \quad \text{if } L_1 < L_2,$$

(15)

where $k$ is an integer, $L_1 = v/(2f_{01})$, $L_2 = v/(2f_{02})$, and $f_{01}$, $f_{02}$ are synchronous frequencies of IDT.

If the condition (14) is satisfied, the maximum of the module characteristics of IDT is equal to the $k$-th passband at the frequency $f_k = f_{01} \pm kf_r$, and while satisfying the condition (15) it is equal to the $k$-th passband at the frequency $f_k = f_{01} - kf_r$.

The passbands of the diluted IDT$_1$ are suppressed significantly except for the passband at the frequency $f_{01}$. For this reason, in Fig. 3b one passband $f_k = f_{01} \pm kf_r = f_{02}$ is presented.

Even narrower passband $\Delta f_r/f_0 = 0.1-0.2\%$ can be realised using two diluted IDTs (Fig. 4a). In this case, it is also possible to have two variants of narrowband filters construction. In the first variant there are the synchronous frequencies of both diluted IDT (or spatial periods of electrodes) being the same, i.e. $f_{01} = f_{02}$, $L_1 = L_2$ and for the spatial periods of groups used for Eq. (16):

$$\frac{L_{ri}}{L_{r2}} = \frac{f_{r2}}{f_{r1}} = \frac{T_{r1}}{T_{r2}} = k/l, \quad \text{and}$$

(16)

When this condition is satisfied, partial passbands of the IDT$_1$ at the frequency $f_k = f_{01} \pm kf_r$ identify with partial passbands of the IDT$_2$ at the frequency $f_k = f_{02} \pm lf_r$ and in the resulting module characteristics of filter there is only one passband at the frequency $f_0 = f_k = f_{1}$ (Fig. 4b).

In the second variant, the spatial periods $L_1$ and $L_2$ are different (Fig. 5a), i.e. $L_1 > L_2$ or $L_1 < L_2$ and the
spatial period of groups of the first \( L_{r1} \) and second \( L_{r2} \) of IDT are an integer multiple of the wavelengths \( \lambda_1 \) and \( \lambda_2 \), corresponding to the synchronous frequencies \( f_{01} \) and \( f_{02} \) of these transducers and they are determined from the relation

\[
\frac{L_{r1}}{L_{r2}} = \frac{L_{r1} \left( \frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right)}{2l + \frac{k}{2}},
\]

where \( k \) and \( l \) are integers.

In the first case \( (L_1 > L_2) \) and in the second \( (L_1 < L_2) \) case, all improper identified partial pass bands are significantly suppressed and belong to the resulting module characteristics of the filter. There is only one desired passband for a synchronous frequency \( f_0 = f_k = f_1 \) (Fig. 5b).

In these constructions of narrowband filters with two diluted IDTs, the operating range of filters can be extended: in the lower part to the values of 0.5 to 1 MHz and less, by using “low-frequency” partial passbands, and in the upper area to the values of 500 to 600 MHz, by using “high-frequency” partial pass bands, without increasing the dimensions of the filter and at the same time without increasing the requirements for the resolution of photolithography.

Construction of diluted IDTs enables retuning of the filter to a variety of synchronous frequencies easily. If metal strips are placed into the gaps between individual groups of diluted IDTs (Fig. 6a), by the change of the width of these strips we can change the speed of the propagation of SAW in the IDT and thus move the partial passband of one or other IDT, the left or right ones. At a certain speed of SAW, there will be identification of some partial pass bands so we can change synchronous frequency of the filter (Fig. 6b). The indicated design allows us to use one photomask to make a variety of different filters with different synchronous frequencies. (The width of the metal strip can be changed with the help of, e.g., chemical etching, laser, etc.).

3. Experimental results

On the basis of the above theory the authors designed, implemented and experimentally verified a few filters and resonators for sensors of non electrical quantities. Below there is an example of the developed filter (it can be used, e.g., for oscillators of common TV distribution, etc.).

A PLF 13 filter has been designed and implemented using Fourier transformation and weighing functions.
Required parameters of PLF 13:
synchronous frequency – 143.5 MHz,
bandwidth “to 3 dB” is ±14 MHz,
group delay – T < 10 ns.

Selected substrate:
Y – cut, Z – the direction of propagation LiNbO₃.

The filter contains the IDT₁ with diluted electrodes
and the broadband IDT₂ with the same spatial period
(L₁ = L₂). The diluted IDT₁ has 42.5 groups made up
of one pair of electrodes, i.e. 85 electrodes. The broad-
band IDT₂ has 11 electrodes, i.e. 5.5 pairs. The spa-
tial period: L = λ₀/2 = 8 µm, period of dilution:
Lᵣ = 2500 µm. Aperture: w = 2300 µm. Synchronous
frequency of the filter f₀ = 143.5 MHz, the inserted
damping: b₈ = 12 dB, quality factor: Q = 650. The de-
sign of the implemented filter is shown in Fig. 7.

A temperature sensor was designed and imple-
mented. One port resonator (Fig. 8) with the electri-
cally shortcircuiting reflector system array PLR40 was
used. It had a lower inserted damping. Thus for further
signal processing we could use a single stage amplifier
of the electrical signal. The calculated, measured pa-
rameters of the resonator and delay line are shown in
Tables 1 and 2.

![Fig. 7. Design of the produced filter.](image1)

![Fig. 8. One port resonator PLR 40.](image2)

### Table 1. Parameters of the implemented acoustoelectronic components (calculated and measured).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>PLF 13</th>
<th>PLO 44</th>
<th>Remark</th>
</tr>
</thead>
<tbody>
<tr>
<td>vₑf [pF/m]</td>
<td>3445</td>
<td>3445</td>
<td></td>
</tr>
<tr>
<td>K²</td>
<td>0.0482</td>
<td>0.0482</td>
<td></td>
</tr>
<tr>
<td>Cₛ' [pF/m]</td>
<td>398.2</td>
<td>434.4</td>
<td>specific capacity of section</td>
</tr>
<tr>
<td>λ₀ [µm]</td>
<td>25</td>
<td>40</td>
<td>λ₀ = vₑf/f₀</td>
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<tr>
<td>lₑ = l₀ [µm]</td>
<td>8</td>
<td>10</td>
<td>electrode and gap width</td>
</tr>
<tr>
<td>f₀ [MHz]</td>
<td>143.5</td>
<td>87.2</td>
<td>calculated</td>
</tr>
<tr>
<td>fᵣM [MHz]</td>
<td>144.2</td>
<td>86.7</td>
<td>measured</td>
</tr>
<tr>
<td>N</td>
<td>85</td>
<td>11</td>
<td></td>
</tr>
<tr>
<td>n</td>
<td>42</td>
<td>5</td>
<td>n = 2N + 1</td>
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<tr>
<td>l' [µm]</td>
<td>2125</td>
<td>440</td>
<td>l = Nλ₀</td>
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<tr>
<td>l [µm]</td>
<td>5225</td>
<td>8650</td>
<td>l = P₀λ₀</td>
</tr>
<tr>
<td>P₀</td>
<td>250</td>
<td>250</td>
<td></td>
</tr>
<tr>
<td>k</td>
<td>250</td>
<td>250</td>
<td></td>
</tr>
<tr>
<td>C_TC [pF]</td>
<td>289</td>
<td>391</td>
<td>C_TC = Cₛ'wN</td>
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<tr>
<td>C_TM [pF]</td>
<td>284</td>
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<tr>
<td>QC</td>
<td>665</td>
<td>768</td>
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<tr>
<td>Qₘ</td>
<td>≈ 650</td>
<td>≈ 780</td>
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</tr>
<tr>
<td>b₈ [dB]</td>
<td>12</td>
<td>18</td>
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</tr>
<tr>
<td>w [µm]</td>
<td>2300</td>
<td>3000</td>
<td>aperture</td>
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Table 2. Parameters of implemented acustoelectronic components (calculated and measured).

<table>
<thead>
<tr>
<th>Parameter</th>
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<tr>
<td>( v_{ef} ) [pF/m]</td>
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<tr>
<td>( K^2 )</td>
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<td></td>
</tr>
<tr>
<td>( C'_s ) [pF/m]</td>
<td>395.9</td>
<td>specific capacity of section</td>
</tr>
<tr>
<td>( \varepsilon )</td>
<td>-0.0241</td>
<td>impedance matching</td>
</tr>
<tr>
<td>(</td>
<td>r</td>
<td>)</td>
</tr>
<tr>
<td>( N )</td>
<td>400</td>
<td>number of elements of the reflection system</td>
</tr>
<tr>
<td>( d ) [mm]</td>
<td>2.39</td>
<td>distance of the apparent plane of reflection</td>
</tr>
<tr>
<td>( m_d )</td>
<td>70</td>
<td></td>
</tr>
<tr>
<td>( s ) [mm]</td>
<td>1.42</td>
<td>distance of the inner edges of the reflection systems</td>
</tr>
<tr>
<td>( m_s )</td>
<td>110</td>
<td></td>
</tr>
<tr>
<td>( R_1 ) [\ Omega ]</td>
<td>29.64</td>
<td>equivalent circuit</td>
</tr>
<tr>
<td>( L_1 ) [\mu H]</td>
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<td></td>
</tr>
<tr>
<td>( C_1 ) [pF]</td>
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</tr>
<tr>
<td>( C_T ) [pF]</td>
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<td>( R_T ) [\ Omega ]</td>
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<tr>
<td>( R_e ) [\ Omega ]</td>
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<td></td>
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<tr>
<td>( f_{ov} ) [MHz]</td>
<td>75.84</td>
<td>series resonance frequency – calculated</td>
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<tr>
<td>( f_{oM} ) [MHz]</td>
<td>76.068</td>
<td>measured</td>
</tr>
<tr>
<td>( f'_{ov} ) [MHz]</td>
<td>76.28</td>
<td>parallel resonance frequency – calculated</td>
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<td>( f'_oM ) [MHz]</td>
<td>76.324</td>
<td>measured</td>
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<tr>
<td>( n_f )</td>
<td>20</td>
<td>number of electrodes IDM</td>
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<tr>
<td>( l_e = l_0 ) [\mu m]</td>
<td>11</td>
<td>electrode and gap width</td>
</tr>
<tr>
<td>( w )</td>
<td>638</td>
<td>aperture</td>
</tr>
<tr>
<td>( Q_sM )</td>
<td>2415</td>
<td>factor quality series resonance</td>
</tr>
<tr>
<td>( Q_{pM} )</td>
<td>2642</td>
<td>factor quality parallel resonance</td>
</tr>
<tr>
<td>( C_{RM} ) [pF]</td>
<td>2.14</td>
<td>static kapacitance rezonator</td>
</tr>
<tr>
<td>( b_d ) [dB]</td>
<td>10</td>
<td>inserted damping</td>
</tr>
</tbody>
</table>

**Required parameters of PLR 40:**

IDM: \( N = 10 \) electrode, \( l_e = l_0 = 11 \mu m \).

Reflection system: \( N = 400 \) electrode, \( l_e = l_0 = 6 \mu m \).

**Selected substrate:**

Y – cut, Z – the direction of propagation LiNbO\(_3\), thickness of the pad – 0.5 mm.

Another actual example of the use of the developed theory was design and implementation of delay lines which have been used for the identification system with the SAW. It had advantages over other systems.

Example of an identification system using the properties of SAW is shown in Fig. 9. It consists of a transmitter, receiver, computer (i.e. evaluation unit), and passive identification card.

The identification card with the code number is located in the observation unit (e.g. a railway wagon, etc.) It can be identified remotely using an impulse transmission system. An impulse transmission system sends a short query high frequency signals to the identification card. Next, after a short delay, the card sends a coded response, which is recorded by the receiver with the phase detector. The transmitter sends short radio impulses with a certain carrier frequency (MHz), duration (typically 0.5 ± 0.1 \mu m) and repeated

Fig. 9. Example of an identification system using the properties of SAW.
frequency (e.g. 3 Hz, etc.). The transmitter range is limited within a few meters (antenna radiation is narrowly directed). Next, the signal is processed in the evaluation unit.

A designed delay line PLO 44 (Fig. 10) consists of an input IDT\(_1\) and an output IDT\(_2\). The transducers are made by using photolithographic technology on the piezoelectric substrate cut \(Y\), \(Z\) direction of propagation of the \(\text{LiNbO}_3\). The two transducers and the loop antenna are connected together. The required selected number in the binary system is obtained by the phase modulation of the signal. The criterion of the design is that the length of the space period \(L_1\) must be greater than the period of the length \(L_2\). By increasing the number of pairs of electrodes it can be expanded by number of possible display numbers. (e.g. the first pair forms a so called start (trigger) bit, followed by a sequence of zeros and ones forming in the binary system a certain number, followed by control of parity, stop bit, etc.).

**Required parameters PLO 44:**

IDM: \(n = 9\) electrodes, \(l_e = l_0 = 10\ \mu\text{m}\), \(n = 2\) electrodes, \(l_e = l_0 = 10\ \mu\text{m}\).

**Selected substrate:**

\(Y\) - cut, \(Z\) - propagation direction, \(\text{LiNbO}_3\), thickness of the pad – 1 mm, \(f_0 = 87.2\ \text{MHz}\).

It can be noticed that:

- An additional requirement for the topology of the filter with the single narrowband diluted IDT and the broadband IDT is maintaining the ratio of the spatial period of groups of the diluted IDT and the length of the broadband IDT. The ratio ensures the suppression of unwanted partial passbands of the module characteristics.
- There were introduced requirements for repetition accuracy of the spatial period of the electrodes and groups for filters with two diluted IDTs. In this way identification of partial passbands at a given frequency and suppression of unwanted pass bands can be fully secured.
- The developed theory of synthesis can be advantageous for both described structural variants of filters, operating on various partial passbands. It can be also used for design and realisation of a wide range of acoustoelectronic components with SAW.
- The proposed theory was used for narrowband filters, delay lines for the single mode oscillators, and resonators.
- The results of the conducted analysis are essential for the development of knowledge in the given scientific field and applications of acoustoelectronic components.
- The authors presented realisation of the acoustoelectronic components.

4. Conclusions

The paper also deals with the surface acoustic waves (SAW) and the theory of synthesis of the asymmetrical delay line with the interdigital transducer with diluted electrodes. The authors developed a theory, design, and implementation of the proposed design. The authors also carried out measurements.

The authors analysed acoustoelectronic components with SAW: PLF 13, PLR 40, delay line with PAV 44 PLO. The filter PLF 13 was used for the oscillator of common television distribution. One port of the resonator PLR 40 was used for application of the temperature sensor (10 dB). The temperature sensor developed on the basis of the delay line has a high attenuation (52 dB). It was necessary to use a multistage amplifier. Next, the delay line and PAV 44 PLO were described and used in the presented identification systems. The presented topic of the paper has potential practical use.
In the future, the authors will analyse other acoustoelectronic components and signals. There is an idea to analyse: other acoustic signals (Lara et al., 2015), acoustic holography (Jozwik, 2016), vibrations (Li et al., 2016; 2017; Krolickzy et al., 2014; Sawczuk, 2017; Sawczuk, Szymanski, 2017), and application of signals for power electronics (Spanik et al., 2013; Frivaldsky et al., 2013).

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Conflicts of Interest

The authors declare no conflict of interest.

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